## ある割当問題とその解法

## ABSTRACT

## A SPECIAL MATCHING PROBLEM AND AN ALGORITHM FOR IT

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This paper deals with the following problem: Suppose there exist n point sets,  $N_1$ ,  $N_2$ , - - -,  $N_n$ , each point p of which has two attribute values A(p) and F(p), where A(p) takes a binary value 'good' or 'bad' and F(p) takes a value of real number given according to some evaluation of p. Then, the problem is to find an interchanging rule so that by repeatedly interchanging attribute values A(p) and F(p) between  $p_1$ ,  $p_2 \in N(N = \bigcup_{i=1}^{n} N_i)$ , the value (1) should be minimized under the condition that the value (2) be maximal:

- (1) Max Max |F(p) F(p)|ieB peN<sub>i</sub>
- (2) Value of |B|
  where,
  - (i)  $B = \{i | A(p) = 'good' \forall p \in N_i \}$
  - (ii) A(p) and F(p) are attribute functions modified by interchanging.

In this paper, the authors have developed a theory by which this problem could be handled as a matching problem for a bipartite graph and presented an efficient algorithm for it.

A numerical example and a result of numerical experiment are also given.